

P132 43, 47, 49, 75, 83

(43)  $\frac{mv^2}{x} = \frac{G M_s m_e}{r^2}$

$$v = \sqrt{\frac{G M_s m_e}{r}} = \sqrt{\frac{(6.67 \times 10^{-11} \text{ Nm}^2 \text{ kg}^{-2})(5.98 \times 10^{24} \text{ kg})}{(6300 \times 10^3 \text{ m} + 6380 \times 10^3 \text{ m})}}$$

$$v = \underline{6300 \text{ ms}^{-1}}$$

(47)  $\frac{mv^2}{r} = \frac{G M m}{r^2}$

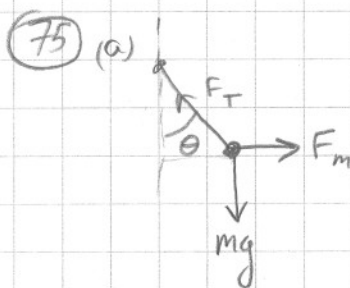
$$v = \sqrt{\frac{G M}{r}} = \sqrt{\frac{(6.67 \times 10^{-11} \text{ Nm}^2 \text{ kg}^{-2})(5.98 \times 10^{24} \text{ kg})}{(6380 \times 10^3 \text{ m} + 8850 \text{ m})}}$$

$$v = \underline{7900 \text{ ms}^{-1}}$$

(49)  $\frac{4\pi^2 r}{T^2} = \frac{G M}{r^2}$

$$T = \sqrt{\frac{4\pi^2 r^3}{G M}} = \sqrt{\frac{4\pi^2 (73000 \times 10^3)^3}{(6.67 \times 10^{-11} \text{ Nm}^2 \text{ kg}^{-2})(5.7 \times 10^{26} \text{ kg})}} = \underline{2.0 \times 10^4 \text{ s}}$$

$$= \sqrt{\frac{4\pi^2 (170000 \times 10^3)^3}{(6.67 \times 10^{-11} \text{ Nm}^2 \text{ kg}^{-2})(5.7 \times 10^{26} \text{ kg})}} = \underline{7.1 \times 10^4 \text{ s}}$$



$$F_T \sin \theta = F_m$$

$$\frac{mg \sin \theta}{\cos \theta} = F_m$$

$$mg \tan \theta = F_m$$

$$mg \tan \theta = \frac{G M m}{D_m^2}$$

$$\theta = \tan^{-1} \left( \frac{G M m}{y D_m^2} \right)$$

$$F_T \cos \theta = mg$$

$$F_T = \frac{mg}{\cos \theta}$$

$$F_m = \frac{G M m}{D_m^2}$$

cont'd

75 cont'd

Now we have to get rid of  $g$  and  $G$

$$Mg = \frac{GMm}{R_E^2}$$

$$\text{So } \frac{G}{g} = \frac{R_E^2}{mE}$$

$$\therefore \theta = \tan^{-1} \left( \frac{R_E^2 m_m}{m_E D_m^2} \right)$$

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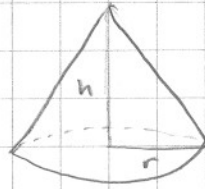
(b) Volume of a cone

$$= \frac{\pi r^2 h}{3}$$

$$= \frac{\pi (2000\text{m})^2 (4000\text{m})}{3}$$

$$= 1.676 \times 10^{10} \text{ m}^3$$

$$m = (3000 \text{ kg m}^{-3})(1.676 \times 10^{10} \text{ m}^3) = \underline{5 \times 10^{13} \text{ kg}}$$



(c)  $D_m = 5000 \text{ m}$

$$\theta = \tan^{-1} \left( \frac{R_E^2 m_m}{m_E D_m^2} \right) = \tan^{-1} \left( \frac{(6380 \times 10^3 \text{ m})^2 (5 \times 10^{13} \text{ kg})}{5.98 \times 10^{24} \text{ kg} (5000 \text{ m})^2} \right)$$

$$\underline{\theta = 8 \times 10^{-4} \text{ degrees}}$$

$$(83) (a) \frac{mv^2}{x} = \frac{G M m}{r^2}$$

$$v = \sqrt{\frac{GM}{r}} = \sqrt{\frac{(6.67 \times 10^{-11} \text{ Nm}^2 \text{ kg}^{-2})(5.98 \times 10^{24} \text{ kg})}{(11000)(1.852 \times 10^3 \text{ m}) + 6380 \times 10^3 \text{ m}}}$$

$$v = 3861 \text{ ms}^{-1} = \underline{3900 \text{ ms}^{-1}}$$

$$(b) v = \frac{2\pi r}{T}$$

$$T = \frac{2\pi r}{v} = \frac{2\pi ((11000)(1.852 \times 10^3 \text{ m}) + 6380 \times 10^3 \text{ m})}{3861 \text{ ms}^{-1}}$$

$$T = \underline{4.4 \times 10^4 \text{ s}}$$