Electric Field, Potential and Energy

Electric Potential

- An electric charge creates an electric field in the space around it
- It also creates a related quantity, an electric potential

Definition

- Electric potential is the work done in moving a positive test charge from infinity (very far away) to a point P near a charge Q

$$V = \frac{W}{q}$$

- Electric potential is measured in units called volts (V)
- 1 V = 1 JC^{-1}

Recall: $W = Fd$ and $F = k\frac{q_1 q_2}{r^2}$

In our case, the displacement, d is r

So… $V = \frac{W}{q} = \frac{Fd}{q} = \frac{kq_1 q_2 r}{r^2 q}$

$$\boxed{V = \frac{kq}{r}}$$

Electric Potential Energy

- If we do work to move a test charge from infinity to a point P near a charge Q, then it has gained energy (potential energy)
- The electric potential energy of the charge is then

$$E_p = qV$$

$$\boxed{V = \frac{E_e}{q}}$$

Potential Difference

- In practice we would like to measure the potential difference between two charges
- In general, the work that must be done on a charge q to move it from point A, where the potential is V_A, to point B, where the potential is V_B, is given by

$$W = \Delta E_p = E_{pB} - E_{pA} = qV_B - qV_A = q(V_B - V_A)$$

$$W = q\Delta V$$

Another Look at Electric Field

- Electric field is related to electric potential energy as follows:

$$E = \frac{\Delta V}{d}$$

- ΔV is the potential difference between the plates
- d is the separation between the plates

- We can also derive an equation for the electric potential energy between the plates

$$V = \frac{E_e}{q} \qquad E = \frac{\Delta V}{d}$$

$$E_e = qV \qquad \Delta V = Ed$$

$$E_e = qEd$$